Modeling Spatial and Temporal Dependencies of User Mobility in Wireless Mobile Networks

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Abstract—Realistic mobility models are fundamental to evaluate the performance of protocols in mobile ad hoc networks. Unfortunately, there are no mobility models that capture the non-homogeneous behaviors in both space and time commonly found in reality, while at the same time being easy to use and analyze. Motivated by this, we propose a time-variant community mobility model, referred to as the TVC model, which realistically captures spatial and temporal correlations. We devise the communities that lead to skewed location visiting preferences, and time periods that allow us to model time dependent behaviors and periodic re-appearances of nodes at specific locations.

To demonstrate the power and flexibility of the TVC model we use it to generate synthetic traces that match the characteristics of a number of qualitatively different mobility traces, including wireless LAN traces, vehicular mobility traces, and human encounter traces. More importantly, we show that, despite the high level of realism achieved, our TVC model is still theoretically tractable. To establish this, we derive a number of important quantities related to protocol performance, such as the nodal spatial distribution, the average node degree, and the hitting and meeting times for the TVC model, and provide examples of how to utilize this theory to guide design decisions in routing protocols.

I. INTRODUCTION

Mobile ad hoc networks (MANETs) are self-organized, infrastructure-less networks that could potentially support many applications, such as vehicular networking (VANET) [25], disaster relief [24], wild-life tracking [26], and Internet provision to rural areas [3], to name a few. As the devices are easily portable and the scenarios of deployment are inherently dynamic, mobility becomes one of the key characteristics in most of these networks. It has been shown that mobility impacts MANETs in multiple ways, such as network capacity [6], routing performance [13], and cluster maintenance [23]. In short, the evaluation of protocols and services for MANETs seems to be inseparable from the underlying mobility models. It is, thus, of crucial importance to have suitable mobility models as the foundation for the study of ad hoc networks.

Ideally, a good mobility model should achieve a number of goals: (i) it should first capture realistic mobility patterns of scenarios in which one wants to eventually operate the network; (ii) at the same time it is desirable that the model is mathematically tractable; this is very important to allow researchers to derive performance bounds and understand the limitations of various protocols under the given scenario, as in [4], [5], [6], [22]; (iii) finally, it should be flexible enough to provide qualitatively and quantitatively different mobility characteristics by changing some parameters of the model, yet in a repeatable and scalable manner; designing a new mobility model for each existing or new scenario is undesirable.

Most existing mobility models excel in one or, less often, two aspects of the above requirements, but none satisfies all of them at the same time. The most widely used mobility models are random mobility models such as random walk, brownian motion, random direction, and random waypoint [8]. Their strength is the theoretical tractability but their weakness is the lack of realism. More complicated synthetic mobility models (e.g., [17], [39], [40]) improve the realism, but most of the time at the expense of theoretical tractability. More recently, a large number of empirical mobility traces from real mobile users have been collected [9], [10], [11], [12], [22]. Although one can use such traces directly in an evaluation with excellent realism, these traces are usually rather inflexible and provide only a single snapshot of the underlying mobility process. To address these two issues, trace-based mobility models [15], [16], [20] have been proposed (i.e. larger, more flexible synthetic traces created from the smaller empirically collected ones). Yet, most of these models do not possess the necessary flexibility to match mobility characteristics of traces other than the ones on which they are based.

The main contribution of this paper is the proposal of a time-variant community mobility model, referred to as the TVC model, which is realistic, flexible, and mathematically tractable. The model captures several important mobility characteristics observed empirically from various WLAN traces [14]. One of the salient characteristics is location preference. In the TVC model, we extend the concept of communities [18] to serve as popular locations for the nodes. Another important characteristic is the time-dependent, periodic behavior of many nodes. To capture this, we implement time periods in which the nodes move differently [1]. To our best knowledge, this is the first synthetic mobility model that captures non-homogeneous behavior in both space and time.

To establish the flexibility of our TVC model we show that we can match its two prominent properties, location visiting preferences and periodical re-appearance, with multiple WLAN traces, collected from environments such as university campuses [12], [14] and corporate buildings [9]. More interestingly, although we motivate the TVC model with the observations made on WLAN traces, our model is generic enough to have wider applicability. We validate this claim by examples of matching our TVC model with two additional mobility traces: a vehicle mobility trace[29] and a human
encounter trace [22]. In the latter case, we are even able to match our TVC model with some other mobility characteristics not explicitly incorporated in our model by its construction, namely the inter meeting time and encounter duration between different users/devices. These quantities are particularly important for encounter-based (or “delay-tolerant” [2]) protocols.

Finally, in addition to the improved realism, the TVC model can be mathematically treated to derive analytical expressions for important quantities of interest, such as the nodal spatial distribution, the average node degree, the hitting time (time required for a mobile node to hit a randomly selected coordinate) and the meeting time (time required for two mobile nodes to come within communication range of each other). These quantities are often fundamental to theoretically study issues such as routing performance, capacity, connectivity, etc. We show that our theoretical derivations are accurate through simulation cases with a wide range of parameter sets, and additionally provide examples of how our theory could be utilized in actual protocol design. To our best knowledge, this is the first synthetic mobility model proposed that matches with traces from multiple scenarios, and has also been theoretically treated to the extent presented in this paper. Due to its strengths in both flexibility and theoretical tractability, the TVC model has two major applications: to generate realistic mobility patterns under a wide range of different scenarios, as we show in section IV, and to facilitate performance analysis and prediction, as we show in section VII. We also make the code of the TVC model available at [30].

The paper is organized as follows: In Section II we discuss related work. Our TVC model is then introduced in Section III. In Section IV, we show how to generate realistic mobility scenarios matched with various traces. Then, in Section V, we present our theoretical framework and derive generic expressions of various quantities. Simulation validates the accuracy of these expressions in Section VI. Additionally, in Section VII, we motivate our theoretical framework further, by applying our analysis to performance predictions in protocol design. Finally, we conclude the paper in Section VIII.

II. RELATED WORK

Mobility models have been long recognized as one of the fundamental components that impacts the performance of wireless ad hoc networks. For example, it is shown that mobility can improve the scaling law of the network capacity with respect to the nodal density to $O(1)$ [6]. Different underlying mobility models also change the performance ordering of various MANET routing protocols [13]. More recently, mobility has been utilized as the enabling factor for message delivery in delay tolerant networks (DTNs[2]), where a complete path from the source node to the destination node does not exist at any time instant, broadening the scenarios in which communication networks can be established.

A wide variety of mobility models are available in the research community (see [8] for a good survey). Among all mobility models, the popularity of random mobility models (e.g., random walk, random direction, and random waypoint) roots in its simplicity. They are not only easy to generate, tune and scale, but also amenable to mathematical analysis. A number of important properties for these models have been studied, such as the stationary nodal distribution [36], the hitting and meeting times [18], and the meeting duration [37]. These quantities in turn enable routing protocol analysis to produce performance bounds [4], [5]. However, random mobility models are based on over-simplified assumptions, and as has been shown recently and we will also show in the paper, the resulting mobility characteristics are very different from real-life scenarios. Hence, it is debatable whether the findings under these models will directly translate into performance in real-world implementations of MANETs.

More recently, an array of synthetic mobility models are proposed to improve the realism of the simple random mobility models. More complex rules are introduced to make the nodes follow a popularity distribution when selecting the next destination [17], stay on designated paths for movements [40], or move as a group [39]. More variants of mobility rules can be found in various models [8]. These rules enrich the scenarios covered by the synthetic mobility models, but at the same time make theoretical treatment of these models difficult. In addition, most synthetic mobility models are still limited to i.i.d. models, and the mobility decisions are also independent of the current location of nodes and time of simulation.

A different approach to mobility modeling is by empirical mobility trace collection. Along this line, researchers have exploited existing wireless network infrastructure, such as wireless LANs (e.g., [9], [11], [12]) or cellular phone networks (e.g., [10]), to track user mobility by monitoring their locations (through their associations with base stations). Such traces can be replayed as input mobility patterns for simulations of network protocols [38]. More recently, DTN-specific testbeds [22], [25], [26] aim at collecting encounter events between mobile nodes instead of the mobility patterns. Some initial efforts to mathematically analyze these traces can be found in [22], [42]. Yet, due to its experimental nature, the size of the traces and the environments in which the experiments are performed can not be adjusted at will by the researchers. To improve the flexibility of traces, the approach of trace-based mobility models have also been proposed [15], [16], [20]. These models discover the underlying mobility rules that lead to the observed properties (such as the duration of stay at locations, the arrival patterns, etc.) in the traces. Statistical analysis is then used to determine proper parameters of the model to match it with the particular trace.

The goal of this work is to combine the strengths of various approaches to mobility modeling and propose a realistic, flexible, and mathematically tractable synthetic mobility model. Our work is partly motivated by a previous work of ours [14] in which we identify several prominent, common properties in multiple WLAN traces. Large-scale deployments of WLANs in university [11], [12] and corporate [9] campuses provide excellent platforms in which huge amount of user data can be collected and analyzed. Resources for measurement-based study are available at two trace archives [27], [28]. We leverage these traces to understand empirical user mobility, and propose the TVC model based on the prominent characteristics observed. This model extends the concept of communities proposed by us in [18] and also introduces time-dependent behavior. A preliminary version of the model has been presented in [1].
We differentiate our work from other trace-based models [15], [16], [20] in several aspects. First, among all efforts of providing realistic mobility models, to our best knowledge, this is the first work to explicitly capture time-variant mobility characteristics. Although capturing time-dependent behavior is suggested in [20], it has not been incorporated in the particular paper. Second, while previous works emphasize the capability to truthfully recreate the mobility characteristics observed from the traces, we also strive to ensure at the same time the mathematical tractability of the model. Our motivation is to facilitate the application of our model for performance prediction of various communication protocols. Finally, although we start from mobility characteristics observed from WLAN traces, we propose a mobility model that has wider applicability — in addition to WLANs, it can be tuned to match with other types of traces, such as a vehicle mobility trace [29], and even with other characteristics in other traces of human mobility (e.g., the encounter duration and the inter-meeting time [22]).

As a final note, in [21], the authors assume the attraction of a community (i.e., a geographical area) to a mobile node is derived from the number of friends of this node currently residing in the community. In our paper we assume that the nodes make movement decisions independently of the others (nonetheless, node sharing the same community will exhibit mobility correlation). Mobility models with inter-node dependency require a solid understanding of the social network structure, which is an important area under development. We plan to work further in this direction in the future.

III. Time-variant Community Mobility Model
A. Mobility Characteristics Observed in WLAN Traces

The main objective of the paper is to propose a mobility model that captures the important mobility characteristics observed in daily life. To better understand this mobility, we have chosen to study a number of wireless LAN traces collected by several research groups (e.g., traces available at [27] or [28]). The reason for this choice is that WLAN traces log information regarding large numbers of nodes, and thus are more reliable for statistical analysis. After analyzing a large number of traces, we have observed two important properties that seem to be recurrent in all of them: skewed location visiting preferences and time-dependent mobility behavior [14].

First, by location visiting preference we mean the amount of time that a node spends associated with a given access point (AP). In Fig. 1(a) we calculate for various traces the fraction of the total online time an average node spends with its most favorite AP, its second favorite AP, etc., up to its least favorite AP. (This is essentially the probability density function of the association time of a node with an AP, with the APs sorted in descending order of total association time.) It is clear from the plot that a node on average spends more than 65% of its online time associated with its favorite AP, and more than 95% of its online time at only five APs. We refer to this behavior by saying that the location visiting preference (or in short “location preference”) of nodes is skewed.

Second, by time-dependent mobility behavior we refer to the fact that nodes tend to behave differently during different times of the day (or even during different days), and most specifically to exhibit some amount of periodicity in terms of the locations they choose to visit. In Fig. 1(b) we plot the probability of a node appearing in the same location at some time in the future, as a function of the difference in time. It is evident from the plot that nodes appear at the same AP with a higher probability after a time-gap of integer multiples of days. This creates the saw-tooth pattern in the curves. A slightly stronger weekly correlation could also be observed in some plots (see for example the slightly larger peak in the MIT curve for a time gap of seven days). It is thus clear that nodes behave differently in different periods in time, and that similar behaviors tend be repeated on a daily basis.

Unfortunately, most existing mobility models fail to capture these two properties. For simple random models, like random direction, random waypoint, random walk, etc., there is obviously no preference in both space and time. This is demonstrated in Fig. 1 by a straight line (uniform distribution) for the Random Direction model for the respective probabilities. Even for more sophisticated models that try to capture other aspects of mobility, such as group mobility in the RPGM model [39] or a model considering obstacles and pathways [40], these two properties would also be straight lines in the plots as spatial and temporal preference is not a part of these models. There do exist some more recent models (e.g., [18], [17], [15], [16]) that aim at capturing spatial preference explicitly. An example of such a model is the simpler community model of [18]. As is shown in Fig. 1(a), with appropriately assigned parameters this model is able to capture the skewed location visiting preference, to some extent. However, time-dependent behavior is not captured, and thus the periodical re-appearance property cannot be reproduced, as shown by the flat curve labeled community model in Fig. 1(b).

It is our goal to design a mobility model that successfully captures both of these two properties observed in the majority of traces. One could argue that a potential shortcoming of this approach is that WLAN traces do not register continuous movement of the devices, but rather associations of users/nodes with specific APs. In addition, some devices are not always on, and typically there are some gaps in the coverage of access points in these networks. However, we believe that the two properties, namely skewed location preference and time-dependency, are prevalent in real-life mobility. This belief is further supported by observing typical daily activities of humans: most of us tend to spend most of the time at a handful of frequently visited locations, and a recurrent daily or weekly schedule is an inseparable part of our lives. As a result, a model supporting location-preference and time-dependent mobility should be able to capture human mobility in many contexts, if carefully designed. Comparison with non-WLAN traces in Section IV confirms our argument.

B. Construction of the Time-variant Community Model

Skewed location preferences arise naturally due to extended stay at locations that bear importance to us, such as homes and offices, cafeterias and libraries. To capture this phenomenon, we construct popular location(s) for the nodes in the simulation field. These locations, or rather geographical areas, we call communities, and we make a node visit its own community more often than other areas. Different nodes can pick different communities, creating nodes with very diverse behaviors.
Furthermore, multiple communities could be defined if a node tends to visit multiple locations with high probability, some of which could also be shared by more than one node (e.g., people working in the same building, libraries, etc.).

Periodical re-appearance at a given location is related to omnipresent schedules in our lives. Almost everyone follows recurrent daily or weekly schedules, and different behaviors based on time-of-day have been observed in many contexts. To capture time-dependent behaviors, we introduce structure in the time domain by the use of time periods. For a given node, we assign several time periods during which it behaves differently. For example, a node may have different communities during different periods or the same communities but different mobility parameters to move between them. To further ensure periodicity, the time period assignment follows a recurrent structure, with the same “time-period” and its respective statistical characteristics occurring, say, for all weekday mornings.

We illustrate the model with an example in Fig. 2. We also use this example to introduce the notations we use (see Table I) in the rest of the paper. As shown in the example, there are $V = 3$ (where $V$ denotes the total number of time periods) time periods TP1, TP2, and TP3 (of duration $T^1$, $T^2$, and $T^3$, respectively). During each time period, there are a number of communities, that is, geographical areas that are heavily visited. These communities can be chosen differently in each time period, as shown by the three sub-plots. Within a given time period $t$, the $j$-th community is denoted as $Comm_j^t$. This is a square geographical area of edge length $C_j^t$. Note that by construction the communities can overlap (as in TP1 in Fig. 2), or one community can even contain the other (as in TP2 in Fig. 2). Finally, the number of communities in each time period may vary. For example, there are 3 communities in total in the first period, 2 in the second one, and 4 in the third period. The total number of communities in period $t$ is denoted as $S^t_t$. This construction allows for maximum flexibility when designing the simulation setup for nodes with different behaviors. As for the structure in time domain, we need to arrange time periods in a re-current sequence (see Fig. 2 or Fig. 3) that corresponds to a daily or weekly schedule.

We now describe how a node moves inside the above construction. Node movement consists of a sequence of epochs. Each of these epochs is a Random Direction movement. In a typical Random Direction epoch, a node chooses at the beginning its speed uniformly in $[v_{min}, v_{max}]$, and a direction (angle) uniformly in $[0, 2\pi]$; it also chooses the length (distance) of movement (usually distributed exponentially with average in the order of the network dimension), and moves towards this direction with the chosen speed and for the chosen distance; at the end of the epoch, the node picks a pause time randomly and then proceeds to the next epoch.

The difference between our community model and the Random Direction model is that in addition to all other parameters, in the community model the node also chooses randomly the community in which the next epoch will be performed. That is, with probability $\pi_j$, the next epoch takes place inside the node’s $j$-th community ($\sum_{j=1}^{S^t} \pi_j = 1$), rather than moving around the whole simulation area randomly, as in the standard Random Direction model. (Note that we usually add superscript $t$ in the notation, i.e. $\pi_j^t$, to denote that these probabilities might change between time periods.) We say the node is in state $j$ when it has an epoch in the $j$-th community. Further, to ensure that a local move is compatible with the local community size, we also scale the local epoch length by drawing it from an exponential distribution with average length $\tilde{L}_j$, that is, in the order of the given community size.

It is important to note that a node can still perform some of its epochs in the whole simulation area, by assigning an additional community that corresponds to the whole simulation field (e.g.

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### Table I

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
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<tbody>
<tr>
<td>$N$</td>
<td>Edge length of simulation area</td>
</tr>
<tr>
<td>$V$</td>
<td>Number of time periods</td>
</tr>
<tr>
<td>$T^t$</td>
<td>Duration of $t$-th time period</td>
</tr>
<tr>
<td>$S^t_j$</td>
<td>Number of communities in time period $t$</td>
</tr>
<tr>
<td>$C_j^t$</td>
<td>Edge length of community $j$ in time period $t$</td>
</tr>
<tr>
<td>$Comm_j^t$</td>
<td>The $j$-th community during time period $t$</td>
</tr>
<tr>
<td>$\pi_j^t$</td>
<td>Probability that the next epoch is performed in community $j$ during time period $t$</td>
</tr>
<tr>
<td>$v_{min}, v_{max}, T$</td>
<td>Minimum, maximum, and average speed</td>
</tr>
<tr>
<td>$D_{max,j}^t, L_j^t$</td>
<td>Maximum and average pause time after each $t$th epoch</td>
</tr>
<tr>
<td>$p_{move,j}^t, p_{pause,j}^t$</td>
<td>Probability that a node is moving (pausing) when being in community $j$ during period $t$</td>
</tr>
<tr>
<td>$p_{pause,j}^t$</td>
<td>Fraction of time the node is in state $j$ (i.e., $p_{move,j}^t = p_{move,j}^t + p_{pause,j}^t$)</td>
</tr>
<tr>
<td>$R^t$</td>
<td>Transmission range of nodes</td>
</tr>
<tr>
<td>$A(a_j^t, b_j^t)$</td>
<td>The overlapped area between $Comm_j^t$ of node $a$ and $Comm_j^t$ of node $b$</td>
</tr>
<tr>
<td>$w_j^t$</td>
<td>A specific relationship between a target coordinate and the communities in time period $t$</td>
</tr>
<tr>
<td>$\Omega^t$</td>
<td>The set of all possible relationships between a target coordinate and the communities in time period $t$</td>
</tr>
<tr>
<td>$P_h(w_j^t)$</td>
<td>Unit-time hitting probability under the specific scenario $w_j^t$</td>
</tr>
<tr>
<td>$P_{hit}(w_j^t)$</td>
<td>Hitting probability for a time period $t$ under specific scenario $w_j^t$</td>
</tr>
<tr>
<td>$P_{hit}^t$</td>
<td>Unit-time meeting probability in time period $t$</td>
</tr>
<tr>
<td>$P_{hit}^t$</td>
<td>Meeting probability for a time period $t$</td>
</tr>
</tbody>
</table>

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1 For all parameters used in the paper, we follow the convention that the subscript of a quantity represents its community index, and the superscript represents the time period index. Note that all parameters used in the paper can be set differently for each node. When necessary, we use a pair of parentheses to include the node ID for a particular parameter, e.g., $C_j^t(1)$ denotes the edge length of the $j$-th community during time period $t$ for node $i$.

2 To allow a node to move randomly among the whole simulation field sometimes, we often allocate one community to be the whole simulation field (e.g., $Comm_1^t$ in period TP1 in Fig. 2).

Note that we could also choose random waypoint or random walk models for the type of movement during each epoch.

4 To avoid boundary effects, if the node hits the community boundary it is re-inserted from the other end of the area (i.e., “torus” boundaries).
Finally, after an epoch, a node pauses for roaming epochs. Comm period three time periods and different numbers of communities in each time period. (Fig. 2) illustrates a generic scenario of time-variant mobility model, with a larger range of realistic mobility instances than a single trace purposes. Rather, the goal is to be able to reproduce a much more complex structure with more communities and time-dependencies. However, our choices are largely guided by the fact that most of the building blocks we utilize to create our mobility model (e.g. random direction epochs, communities, etc.) are easy to understand, and have been shown to be amenable to theoretical analysis. This will become evident in Section V. At the same time, we will show next that these choices do not compromise our model’s ability to accurately capture real life mobility scenarios.

IV. GENERATION OF MOBILITY SCENARIOS

The TVC model described in the previous section provides a general framework to model a wide range of mobility scenarios, and provides a powerful tool for simulation-based protocol or service evaluations in MANETs. We have made our mobility trace generator available at [30]. The tool provides mobility traces in both ns-2[31] compatible format and time-location (i.e., (t, x, y)) format.

In this section, our aim is twofold: (i) first, we would like to demonstrate the model’s flexibility and how it can be configured to generate mobility instances that are representative of various target wireless networks such as WLANs, VANETs, etc.; (ii) at the same time, we would like to validate the model’s “realism” or “accuracy” by explicitly comparing mobility instances produced by our model with real mobility instances captured in well-known, publicly-available traces. However, it is important to note that the use of such a model is not merely to match it with any specific trace instance available; this is only done for validation and calibration purposes. Rather, the goal is to be able to reproduce a much larger range of realistic mobility instances than a single trace can provide.

We first outline here some general guidelines about how to use the model in order to construct specific mobility scenarios. Then, we show how to explicitly configure the TVC model in order to match the mobility characteristics observed in three case studies: a wireless LAN trace, a vehicular trace, and a human-encounter trace. All the parameter values we use in the examples in this section are also available at [30].

**STEP 1: Determine the structure in Space and Time** The first step to construct the TVC model for a given scenario is to setup the communities and the time period structure. If the map of the target environment is available, one should observe the map and identify the points of attractions in the given environment and how they vary with respect to time (e.g., restaurants on campus during lunch time, hotels in an amusement park during nights), and assign the communities/time periods in the TVC model accordingly. If the map is not available, alternatively, one could use the general mobility characteristics observed in typical traces for the particular target network (as shown, for example, in Fig. 1) as guidelines to assign the structure in space and time. For example, from location preference curves in Fig. 1(a), one can determine the number of communities one needs to explicitly create; as a very simple example, if in most WLAN traces it is observed that the typical node spends say 95% of its time at around 2 to 5 preferred locations (depending on the node), then one could assign each node to have from 2 to 5 local communities in the network (with the actual number and locations of communities randomly chosen for each node), with a larger (roaming) community representing the rest of the 5% of mobility time.

Similarly, from curves like the ones in Fig. 1(b), one may observe the re-appearance periodicity and decide on the time period structure accordingly. If a finer time granularity is necessary (e.g. time-of-day) one could additionally observe the mobility characteristics (e.g. location preferences) on an hour-by-hour basis and identify clear changes in a node’s daily behavior.

**STEP 2: Assign Community-related Parameters** Ideally, for a given environment, once the communities are identified, the related parameters (e.g., \( \pi_j^t, D_j^t, L_j^t \), which represent the probability, average pause time, and average epoch length, at community \( j \) during time period \( t \)) could be assigned according to the mobile nodes’ behavior in each community (e.g., how long does a typical person spend at the cafeteria for lunch?). Nevertheless, in most cases such information is not available, or extremely difficult to obtain. Hence, one could again resort to measured statistics from typical traces to guide the assignment of the parameters. Typically, the attraction of the communities (\( \pi_j^t \)) and the time spent in each community (related to \( D_j^t, L_j^t \)) determine the shape of the location visiting preference curve. Thus, one can use basic probability theory to calculate the expected fraction of time a node spends in a given community as a function of these parameters, and derive from it the values needed to obtain a given location preference profile observed in a curve in Fig. 1(a). We calculate these community stay probabilities later in our implementation.

\(^3\)In reality, one may be able to capture more complex structures with more communities or structure between them, by combining knowledge from the actual network area (map), generic mobility characteristics, and other information about the network.
STEP 3: Assign User On-off Behavior

Note that the mobility trace generated by the TVC model is an “always-on” mobility trajectory of the mobile node (i.e., the node is always present somewhere in the simulation field). Depending on the target environment, this always-on behavior may not be realistic. In many empirically collected traces, not all nodes are present all the time (i.e., some of the nodes are “off” or not in the observed area sometimes). This is the case in two of the scenarios we discuss below - in the WLAN traces, nodes are “on” only when they are not moving; in the vehicle mobility trace, nodes are “on” when they are moving. Thus, before producing the final synthetic trace, assumptions about when the user is considered “on” should sometimes be made and superimposed to the synthetic mobility traces. We apply this step to the traces of the two scenarios mentioned above.

Next, we look into three specific case studies, namely a set of WLAN traces, a vehicular trace, and a trace of inter-node encounters. We show how to apply the fore-mentioned procedure in each case, and show that synthetic mobility traces produced by the TVC model successfully match the characteristics observed in the real traces.

1) Matching Mobility Characteristics with WLAN Traces:

In the first example, we show that the TVC model can re-create the location preferences and re-appearance probability curves observed in WLANs. We construct our synthetic trace from the TVC model with the following steps: (STEP1) We divide the simulation area into a 10-by-10 grid and use these 100 grid cells as the locations for the purpose of measuring mobility statistics for the simulated nodes. For each node, we assign some of the grids to serve as the node’s communities during each time period, according to the method described earlier. (STEP2) We use the mobility characteristics obtained from the WLAN traces (i.e., curves in Fig. 1(a)) to calculate the attraction from the communities (πj) and the pause times of the node (Dj) to shape a decaying tail of location visiting preference. (STEP3) Since devices are usually turned off when users move them (especially for long-range movements between locations) in the real WLANs, we make a similar assumption that the mobile nodes are considered “on” only when they are not moving. When the simulated node moves, we assume that it is not associated with the grid. Note that the curves in Fig. 1(b) represent the probability of an “on” node associated with the same community after the given time gap, and the peaks appear when the considered points in time are in the same type of time period. Therefore, the peak value is \( \sum_{j=1}^{N} \pi_j (P_{on,j})^2 \), where \( P_{on,j} \) denotes the probability a node is considered “on”. Hence, the fraction of time nodes spend on moving \( (L_j/\pi) \) and pause \( (D_j) \) can be adjusted (note that in this case, \( P_{on,j} = D_j / (D_j + L_j/\pi) \)) to change the peak values in the curve of periodical re-appearance property to match with the curves in Fig. 1(b).

We use the MIT WLAN trace (first presented in [9]) as an example to display the match between the synthetic trace derived from the TVC model and the real trace. We also achieved good matching with the USC[14] or the Dartmouth[12] traces, but do not show it here due to space limitations (see [30]). We show the skewed location visiting preferences and the periodical re-appearance properties in Fig. 4 (a) and (b), respectively. We first try a simple synthetic model (labeled as model-simplified, using the parameters of Model-I in Table II) with one community in two time periods. While this simple model captures the major trends in the mobility characteristics, there are several noticeable differences. First, since there is only one community, the tail in the model-simplified curve in Fig. 4(a) is “flat” as opposed to the exponentially diminishing tail of the MIT curve (notice the Y-axis in Fig. 4(a) is in log scale). Second, the peaks in the model-simplified curve in Fig. 4(b) are of equal heights, due to the simple two-alternating-time-period structure, as opposed to varying peak values of the MIT curve. We can improve the matching between the synthetic trace and the real trace by adding complexity in both space (using more communities) and time (using more complex schedule, such as the weekly schedule shown in Fig. 3). In a refined model labeled as Model-complex in Fig. 4, we show that the resulting mobility characteristics match very closely with the MIT trace. This also demonstrates the flexibility of our model - the user can adjust its complexity by choosing the number of communities and time periods needed to achieve a desired level of matching with the mobility characteristics.

2) Matching Mobility Characteristics with Vehicle Mobility Traces:

In this example we display that skewed location visiting preferences and periodical re-appearance are also prominent mobility properties in vehicle mobility traces. We obtain a vehicle movement trace from [29], a website that tracks participating taxis in the greater San Francisco area. We process a 40-day trace obtained between Sep. 22, 2006 and Nov. 1, 2006 for 549 taxis. We obtain the mobility characteristics of the taxis by the following steps. For each taxi, we first identify its movement range within the 40-day period, then draw a rectangular area that bounds the movement of the taxi, and divide this area into equal-sized 10-by-10 grids. We tally the mobility statistics of the taxis using these 100 grids as locations, and show the results in Fig. 5 with the label Vehicle-trace. It is interesting to observe that the trend of vehicular movements is very similar to that of WLAN users in terms of these two properties.

We further show that, using the outlined procedures, we can generate a synthetic trace with similar mobility characteristics as the vehicle mobility trace. After observing the trace closely, we discover that the taxis are offline (i.e., not reporting their locations) when not in operation. Hence in the synthetic trace we make the corresponding assumption (in STEP3) that the nodes are associated with the current grid they reside in only when they are moving; we then consider the pause times as breaks in the taxi operation (hence
meeting probability (see, e.g., Eq. (14)), hence reducing inter-
rate of various tasks (e.g. geographic routing [34]) in mobile
meeting times. Since the devices used to collect the encounter
tances are always-on, we do not apply any changes to the
synthetic trace in STEP 3. We randomly generate 820 pairs of
users and obtain their corresponding distributions of the inter-
meeting time and the encounter duration. These distributions
are shown in Fig. 6 with label Model. It is clear that our
TVC model has the capability to reproduce the observed
distributions, even if it is not constructed explicitly to do so.
This displays its success in capturing the decisive factors of
typical human mobility.

It is clear from the cases studied here that, once we observe
the target environment closely and come up with the right
underlying parameters, the TVC model is able to capture the
consequent mobility characteristics well. In addition, with the
respective configuration, it is possible to generate synthetic
traces with much larger scale (i.e., more nodes) than the
empirical ones while maintaining the same mobility charac-
teristics. It is also possible to generate multiple instances of
the synthetic traces with the same mobility characteristics to
complement the original, empirically collected trace.

V. THEORETICAL ANALYSIS OF THE TVC MODEL

So far, we have established the strength and flexibility of the
TVC model in terms of its ability to reproduce the properties
observed in real mobility traces. Although other proposed
models have also managed to match some sets of collected
measurements [15], [16], [20], none of the existing works has
been shown to capture the variety of qualitatively different
traces (e.g. WLAN, vehicles, inter-contacts) that the TVC
model does. Yet, one of the biggest advantages of our model is
that, in addition to the realism, it is also analytically tractable
with respect to some important quantities which determine
protocol performance. In the rest of this paper, we focus on
demonstrating this last point.

We start here by deriving the theoretic expressions of
various properties of the proposed mobility model. We first
calculate the nodal spatial distribution. This can be represen-
ted as a two-dimensional probability density function of
nodes at any given point in the space. The expected number
of nodes in an area is then calculated by integrating the density
function. This property provides a basic demographic profile
of the simulation area, and can also help to evaluate whether
the model reflects the target environment. Then, we derive the
average node degree, which is the average number of nodes
residing within the communication range of a given node. This
is a quantity of interest due to its implication on the success
rate of various tasks (e.g. geographic routing [34]) in mobile
ad hoc networks. Finally, we derive the expected hitting and

\[ P_{on,j} = \frac{(L_j^i/\tau)}{(D_j^i + L_j^i/\tau)} \] in this case), from which we
can calculate or adjust the respective model parameters. The
curves in Fig. 5 with label Model correspond to the mobility
characteristics of the synthetic trace. As a final note, although
vehicular movements are generally constrained by streets and
our TVC model does not capture such microscopic behaviors,
designated paths and other constraints could still be added in
the model’s map (for vehicular or human mobility) without
losing its basic properties. We defer this for future work.

3) Matching Contact Characteristics with Encounter-based
Traces: In this example, we show that the TVC model is
generic enough to also reproduce the distributions of the
inter-meeting time and the encounter duration observed from
a human encounter trace [22], by setting up its parameters
properly. Specifically, we tune our mobility model to mimic
the behaviors observed in an experiment performed at INFO-
COM 2005 [22]. In this experiment, wireless devices were
distributed to 41 participants of the conference, with appropri-
ate software installed that could log encounters between nodes
(i.e. coming within Bluetooth communication range), as they
moved around the premises of the conference area.

The inter-meeting time and the encounter duration distrib-
ations of all 820 pairs of users obtained from this trace
are shown in Fig. 6 with label Cambridge-INFOCOM.trace.
To mimic such behaviors using our TVC model, we observe
the conference schedule at INFOCOM, and set up a daily
recurring schedule with five different types of time periods
(STEP 1): technical sessions, coffee breaks, breakfast/lunch
time, evening, and late night (see [30] for the detailed par-
eters). For each time period we set up communities as the
conference rooms, the dining room, etc. We also generate a
community that is far away from the rest of the communities
for each node and make the node sometimes isolated in this
community to mimic the behavior of patrons skipping part of
the conference. It is interesting to note that the inter-meeting
time distribution has a sharp drop (the “knee” in the curve) at
16 hours, which is approximately the time gap between the
end of the day and the beginning of the subsequent day at
the conference. This suggests the nodes (naturally) meet
with lower probability during the nights, and thus the time-
dependent mobility provided by our TVC model is appropriate.
We can naturally achieve this by assigning nodes to disjoint
communities (i.e., the “hotel rooms”) during the nights. In
STEP2, we use the theory presented in section V to adjust the
parameters and shape the inter-meeting time and encounter
duration curves. For example, a stronger tendency for nodes to
choose roaming epochs (setting larger \( \pi_r \)) would increase the
meeting probability (see, e.g., Eq. (14)), hence reducing inter-

![Fig. 5. Matching mobility characteristics of the synthetic trace to the vehicle mobility trace.](image)

![Fig. 6. Matching inter-meeting time and encounter duration distributions with the encounter trace.](image)
meeting times for our model. The hitting time is the time it takes a node, starting from the stationary distribution, to move within transmission range of a fixed, randomly chosen target coordinate in the simulation field. The meeting time is the time until two mobile nodes, both starting from the stationary distribution, move into the transmission range of each other. These two quantities are of interest due to their close relationship to the performance of DTN routing protocols, or in general the performance of processes that rely on node encounters. Knowing the meeting time for a mobility model is, for example, crucial when using a “mobility-assisted” or “store-carry-and-forward” protocol to deliver a message [4], [5], while hitting times might be needed if some nodes in the network are static (e.g., sensors, base stations, etc.).

We note that a preliminary version of some of the theoretical derivations presented here appear for a special case of our TVC model only in [1] (that model included one community and two time periods only). Here, we generalize all derivations for any community and time-period structure. Moreover, we present some additional results regarding the spatial distribution and the average node degree that are relevant to various wireless communication protocols, as we show in Section VII. We start with a useful lemma that calculates the probability of a node to reside in a particular state.

**Lemma 5.1:** The probability that a node moves or pauses (after the completion of an epoch) in state $j$, at any given time instant during time period $t$, is:

$$
P_{\text{move},j}^t = \pi_j^t \left( \frac{1}{v_j^t} + D_j^t \right), \tag{1}
$$

$$
P_{\text{pause},j}^t = \pi_j^t \left( \frac{1}{v_j^t} + D_j^t \right). \tag{2}
$$

**Proof:** The result follows from the ratio of the average durations of the moving part ($\frac{1}{v_j^t}$) and the pause part ($D_j^t$) of each state, weighted by the probabilities of choosing the state.

Note that the above stationary probabilities can be calculated for each time period and node separately. We use $P_j^t(i)$ to denote the probability that node $i$ is in state $j$ during time period $t$ (i.e., $P_j^t(i) = P_{\text{move},j}^t(i) + P_{\text{pause},j}^t(i)$).

**A. Derivation of the Nodal Spatial Distribution**

We start with the derivation of the nodal spatial distribution. This becomes relatively straightforward after we observe that a node follows a basic random mobility model (i.e., random direction) in each community. Hence, when a given node is in state $j$, it appears equally likely in any point within $\text{Comm}_j$.

**Theorem 5.2:** For a given area $A$, the probability for a node to appear in $A$ at any given time instant during time period $t$ is

$$
\int_A p(x,y) \, dx \, dy, \tag{3}
$$

where the function $p(x,y)$ is the spatial density function,

$$
p(x,y) = \sum_{\{\forall j \mid (x,y) \in \text{Comm}_j\}} P_j^t / C_j^t. \tag{4}
$$

**Proof:** A node could appear at a given point in space when it is in state $j$ if and only if the $j$-th community includes the point. Within the community, the appearance probability of the node is uniformly distributed. Considering a given point $(x, y)$, the probability for a node to appear at the point is the sum of the contributions from all of its communities that contain the point.

Note that the nodal spatial distribution for each time period is independent, hence can be calculated separately with the above Theorem.

**B. Derivation of the Average Node Degree**

The average node degree of a node is defined as the expected number of nodes falling within its communication range. Each node contributes to the average node degree independently, as nodes make independent movement decisions.

**Lemma 5.3:** Consider a pair of nodes, $a$ and $b$. Assume further that, in time period $t$, community $j$ of node $a$ and community $k$ of node $b$ overlap with each other for an area $A(a_j^t, b_k^t)$. Then, the contribution of node $b$ to the average node degree of node $a$, when $a$ resides in its $j$-th community and $b$ resides in its $k$-th community, is given by

$$
\frac{\pi K^2}{C_j^t(a)} A(a_j^t, b_k^t), \tag{5}
$$

where $K$ is the communication range of the nodes.

**Proof:** Since nodes are uniformly distributed within each community, the probability for node $b$ to fall in the $j$-th community of node $a$ is simply the ratio of the overlapped area over the size of the $k$-th community of node $b$. Node $a$ covers any given point in its community equal-like, hence given node $b$ is in the overlapped area, it is within the communication range of node $a$ with probability $\pi K^2 / C_j^t(a)$.

Following the same principle in Lemma 5.3, we include all community pairs and arrive at the following Theorem.

**Theorem 5.4:** The average node degree of a given node $a$ is

$$
\sum_{\forall j \in \text{Comm}_j^a} P_j^t(a) \sum_{\forall b \in \text{Comm}_j^b} P_j^t(b) \frac{\pi K^2}{C_j^t(a) C_k^t(b)} A(a_j^t, b_k^t). \tag{6}
$$

**Proof:** Eq. (6) is simply a weighted average of the node degree of node $a$ conditioning on its states. For each state with probability $P_j^t(a)$, the expected node degree is a sum over all other nodes’ probability of being within the communication range of node $a$, again conditioning on all possible states.

**Corollary 5.5:** In the special case when all nodes choose their communities uniformly at random among the simulation field, Eq. (6) degenerates to $\sum_{\forall b} \frac{\pi K^2}{C_k^t(b)}$.

**Proof:** This result follows from the fact that a randomly chosen community is anywhere in the simulation field equally likely. See the technical report[30] for details.

Similar to the nodal spatial distribution, the average node degree can be calculated for each time period separately.

**C. Derivation of the Hitting Time**

The sketch of the derivation of the hitting time is as follows: (1) We first condition on the relative location of the
target coordinate with respect to a node’s communities (e.g., whether the target is inside or outside of each community, etc.). We thus have to derive the hitting time for each sub-case separately. (2) We then derive the unit-step probabilities of hitting a target, \( P_h \), for a given sub-case. The unit-step probability is the probability of encountering the target exactly within the next time-unit (rather than within the duration of a whole epoch). In other words, we approximate the continuous mobility with a discrete version of it where nodes move in discrete steps. It has been shown in [18] that the latter provides a good approximation for the continuous version, and is easier to analyze for our purposes. (3) The expected hitting probability for a whole time period, \( P_h \), is then calculated for each sub-case from the unit-step probability, by assuming “hitting” occurs independently in each time step. (4) Finally, taking the weighted average of each sub-case (i.e. weighted by probability of a given target being located inside a given community) we get the overall hitting time.

The most influential factor for the hitting time is whether the target coordinate is chosen inside the node’s communities. We denote the possible relationships between the target location and the set up of communities during time period \( t \) as the set \( \Omega^t \). Note that the cardinality of set \( \Omega^t \) is at most \( 2^{|S_t|} \) (i.e. for each of the \( S_t \) communities, the target coordinate is either in or out of it). Also, not all of the \( 2^{|S_t|} \) combinations are always valid. For example, in the set up of time period 2 in Fig. 2, the communities are overlapped, hence if the target is within \( Comm^2 \) it must be within \( Comm^3 \).

Lemma 5.6: By the law of total probability, the average hitting time can be written as

\[
HT = \sum_{w^1, w^2, ..., w^V \in \Omega^t} P(w^1, ..., w^V) HT(w^1, ..., w^V),
\]

where \( w^1, w^2, ..., w^V \) denote one particular relationship (i.e. a combination of \{out, in\} \( |S_t| \)) between the target coordinate and the community set up during time period 1, 2, ..., \( V \), respectively. Functions \( P(\cdot) \) and \( HT(\cdot) \) denote the corresponding probability for this scenario and the conditional hitting time under this scenario, respectively. Note that each sub-case \{\( w^1, w^2, ..., w^V \)\} is disjoint from all other sub-cases.

To evaluate Eq. (7), we need to calculate \( P(w^1, ..., w^V) \) and \( HT(w^1, ..., w^V) \) for each possible sub-case \( (w^1, ..., w^V) \).

Lemma 5.7: If the target coordinate is chosen independent of the communities and the communities in each time period are chosen independently from other periods, then

\[
P(w^1, ..., w^V) = \prod_{i=1}^{V} P(w^i),
\]

where \( P(w^i) = A(w^i)/N^2 \), i.e., the probability of a sub-case \( w^i \) is proportional to the area \( A(w^i) \) that corresponds to the specific scenario \( w^i \), which is a series of conditions of the following type: \{\{target \in comm^i\}, \{target \not\in comm^i\}\}, ..., \{target \in comm^i\}.

Proof: The result follows from simple geometric arguments.

The first step for calculating \( HT(w^1, ..., w^V) \) is to derive the unit-time hitting probability in time period \( t \) under target coordinate-community relationship \( w^i \), denoted as \( P_h^i(w^i) \).

Lemma 5.8: For a given time period \( t \) and a specific scenario \( w^i \),

\[
P_h^i(w^i) = \sum_{j=1}^{s^t} I(target \in Comm^i_j | w^i) P_{move,j} 2K\pi_j/C_j^2,
\]

where \( I(\cdot) \) is the indicator function.

Proof: The overall unit-time hitting probability is the sum of the hitting probabilities contributed by epochs in each state. Note that the hitting event can only occur when the node is physically moving, and the node can hit the target when it is moving in its \( j \)-th community only if the target coordinate is within the community. When a node moves with average speed \( \pi_j \) in community \( j \), on average it covers a new area of \( 2K\pi_j \) in unit time. Since a node following random direction movements visits the area it moves about with equal probability, and the target coordinate is chosen at random, it falls in this newly covered area with probability \( 2K\pi_j/C_j^2 \) [18]. Hence the contribution to the unit-time hitting probability by movements made in state \( j \) is \( P_{move,j} 2K\pi_j/C_j^2 \), i.e., when the node moves in community \( j \) and the target is in the newly covered area in the time unit.

Note that the movement made in each time unit does not increase or decrease the probability of hitting the target in the subsequent time units, therefore each time unit can be considered as an independent Bernoulli trial with success probability given in Eq. (9). The corollary below immediately follows.

Corollary 5.9: The probability for at least one hitting event to occur during time period \( t \) under scenario \( w^i \) is

\[
P_h^i(w^i) = 1 - (1 - P_h^i(w^i))^T^t.
\]

Finally, using the law of total probability, we derive the conditional hitting time under a specific target-community relationship, \( HT(w^1, ..., w^V) \).

Theorem 5.10:

\[
HT(w^1, ..., w^V) = \sum_{i=1}^{V} HT(w^1, ..., w^V | first hit in period t) \cdot P(w^1, ..., w^V, first hit in period t),
\]

where the probability for the first hitting event to happen in time period \( t \) is

\[
P(w^1, ..., w^V, first hit in period t) = \prod_{i=1}^{V} (1 - P_h^i(w^i)) \cdot P_h^i(w^i) / P
\]

and the hitting time under this specific condition is

\[
HT(w^1, ..., w^V | first hit in period t) = \sum_{i=1}^{V} T^i \cdot (1/\hat{p} - 1) + \sum_{i=1}^{V} T^i + \frac{1}{P_h^i(w^i)}.
\]

\(^6\)This assumption of independence is shown in [18] to be a good approximation, when the expected length of an epoch is in the order of the square root of the area of the community the epoch takes place in.

\(^7\)We neglect the small probability that the target is chosen out of the community but close to it, and make the contributions from epochs in state \( j \) zero if the chosen target coordinate is not in community \( j \).
where \( P = 1 - \prod_{i=1}^{V}(1 - P_{Mi}(w^t)) \) is the hitting probability for one full cycle of time periods.

**Proof:** Eq. (12) holds as each cycle of time periods follows the same repetitive structure, and for the first hitting event to occur in time period \( t \) it must not occur in time period \( 1, ..., (t - 1) \). The first term in Eq. (13) corresponds to the expected duration of full time period cycles until the hitting event occurs. Since for each cycle the success probability of hitting the target is \( P \), in expectation it takes \( 1/P \) cycles to hit the target, and there are \( 1/P - 1 \) full cycles. The second term in Eq. (13) is the sum of duration of time periods before the time period \( t \) in which the hitting event occurs in the last cycle. Finally, the third term is the fraction of the last time period before the hitting event occurs. Note that the last part is an approximation which holds if the time periods we consider are much longer than unit-time.

**D. Derivation of the Meeting Time**

The procedures of the derivation of the meeting time is similar to that of the hitting time detailed in the last section. In short, we derive the unit-step (or unit-time) meeting probability, \( P_m \), and the meeting probability for each type of time period, \( P_M \), and put them together to get the overall meeting time in a similar fashion as in Theorem 5.10.

Similar to Lemma 5.8, we add up the contributions to the meeting probability from all community pairs from node \( a \) and \( b \) in the following Lemma.

**Lemma 5.11:** Let community \( j \) of node \( a \) and community \( k \) of node \( b \) overlap with each other for an area \( A(a_j, b_k) \) in time period \( t \). Then, the conditional unit-time meeting probability in time period \( t \) when node \( a \) and \( b \) are in its community \( j \) and \( k \), respectively, is

\[
P_m(a^t_j, b^t_k) = P_{move,j}(a^t_a, b^t_k)P_{move,k}(b^t_k) + P_{move,j}(a^t_a, b^t_k)P_{stop,k}(b^t_k) + P_{stop,j}(a^t_a, b^t_k)P_{move,k}(b^t_k)
\]

**Proof:** Equation (14) consists of two parts:

(I) Both of the nodes are moving within the overlapped area. This adds the first term in Eq. (14) to the meeting probability. The two ratios, \( A(a^t_j, b^t_k)/C_j^t(a) \) and \( A(a^t_j, b^t_k)/C_k^t(b) \), capture the probabilities that the nodes are in the overlapped area of the communities.

The contribution to the unit-time meeting probability is the product of probabilities of both nodes moving within the overlapped area and the term \( 2K\pi \), which reflects the covered area in unit time. We use the fact that when both nodes move according to the random direction model, one can calculate the effective (extra) area covered by assuming that one node is static, and the other is moving with the (higher) relative speed between the two. This difference is capture with the multiplicative factor \( v \) [18].

(II) One node is moving in the overlapped area, and the other one pauses within the area. This adds the remaining two terms in Eq. (14) to the unit-time meeting probability. These terms follow similar rationale as the previous one, with the difference that now only one node is moving. The second term corresponds to the case when node \( a \) moves (and \( b \) is static), and the third term corresponds to the case when node \( b \) moves (and \( a \) is static).

The derivation of the unit-time meeting probability between nodes \( a \) and \( b \) for time period \( t \) includes all possible scenarios of community overlap. If node \( a \) has \( S^i(a) \) communities and node \( b \) has \( S^i(b) \) communities, there can be at most \( S^i(a)S^i(b) \) community-overlapping scenarios in time period \( t \).

Note that (14) is the general form of Equation (13) and (14) in [1]. If we assume perfect overlap and a single community from both nodes, we arrive at (14). If we assume no overlap, we result in (13). Also note in the general expressions presented in this paper, the whole simulation area is also considered as a community. Therefore we do not have to include a separate term to capture the roaming epochs.

**Corollary 5.12:** The probability for at least one meeting event to occur during time period \( t \) is

\[
P_M^t = 1 - \prod_{\forall (j,k)} P_{ov}(a^t_j, b^t_k) \cdot (1 - P_m(a^t_j, b^t_k))^T,
\]

where \( P_{ov}(a^t_j, b^t_k) \) is the probability that the community \( j \) of node \( a \) overlaps with community \( k \) of node \( b \). This quantity is simply 1 if the communities have fixed assignments and \( A(a^t_j, b^t_k) \neq 0 \). If the communities are chosen randomly, this probability can be derived by Lemma 4.5 in [1]. Due to space constraint, the Lemma is not reproduced here.

Finally, similarly to Theorem 5.10, the expected meeting time can be calculated using the results in the Lemmas in this section.

**Theorem 5.13:** The expected meeting time is

\[
MT = \sum_{i=1}^{V} MT(\text{meet in period } t)P(\text{meet in period } t).
\]

Where the quantities in the above equation are calculated by

\[
P(\text{meet in period } t) = \prod_{i=1}^{V}(1 - P_{Mi}(w^t)) \cdot P_M^t,
\]

\[
MT(\text{meet in period } t) = \sum_{i=1}^{V} T^i \cdot \left( \frac{1}{Q} - 1 \right) + \sum_{i=1}^{t-1} T^i + \frac{1}{P_m},
\]

where \( Q = 1 - \prod_{i=1}^{V}(1 - P_{Mi}(w^t)) \) is the meeting probability for one full cycle of time periods.

**Proof:** The proof is parallel to that of Theorem 5.10 and is omitted due to space limitations (see [30] for details).

**VI. VALIDATION OF THE THEORY WITH SIMULATIONS**

In this section, we compare the theoretical derivations of the previous section against the corresponding simulation results, for various parameter settings. Through extensive simulations with multiple scenarios and parameter settings, we establish the accuracy of the theoretical framework. Due to space limitations, we can only show some examples of the simulation results we have. More complete results can be found at [30].
We use the same movement speed for all nodes: $v_{\text{max}} = 15$ and $v_{\text{min}} = 5$ in all scenarios. In all cases we use two time periods and they are named as time period 1 and 2 for consistency. We only list the parameters for the simple models (Model 1–4) here. Please refer to [30] for the details of the generic models (Model 5–7).

### Table II

<table>
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<th>Model name</th>
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<th>$C_2$</th>
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<th>$D_{\text{max}, r}$</th>
<th>$L_1$</th>
<th>$L_2$</th>
<th>$\pi_1$</th>
<th>$\pi_2$</th>
<th>$\pi_3$</th>
<th>$T^1$</th>
<th>$T^2$</th>
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<td>100</td>
<td>100</td>
<td>50</td>
<td>80</td>
<td>320</td>
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<td>0.286</td>
<td>0.8</td>
<td>0.2</td>
<td>5760</td>
</tr>
<tr>
<td>Model 2</td>
<td>Highly attractive communities</td>
<td>1000</td>
<td>200</td>
<td>50</td>
<td>100</td>
<td>200</td>
<td>52</td>
<td>320</td>
<td>0.067</td>
<td>0.333</td>
<td>0.889</td>
<td>0.111</td>
<td>3000</td>
</tr>
<tr>
<td>Model 3</td>
<td>Not attractive communities</td>
<td>1000</td>
<td>100</td>
<td>100</td>
<td>50</td>
<td>200</td>
<td>80</td>
<td>320</td>
<td>0.5</td>
<td>0.5</td>
<td>0.667</td>
<td>0.333</td>
<td>2000</td>
</tr>
<tr>
<td>Model 4</td>
<td>Large-size communities</td>
<td>1000</td>
<td>200</td>
<td>250</td>
<td>50</td>
<td>100</td>
<td>200</td>
<td>320</td>
<td>0.7</td>
<td>0.3</td>
<td>0.889</td>
<td>0.111</td>
<td>2000</td>
</tr>
</tbody>
</table>

We summarize the parameters for the tested scenarios in Table II. We use two different setup of the TVC model for the simulation cases. The parameters listed in Table II are for the simple models (Model 1–4), where we have two time periods with two communities in each time period (one of the communities is the whole simulation field). We also simulate for more generic setup of the TVC model (Model 5–7, refer to [30] for its parameters), where we have three communities (one of them is the simulation field) in each time period. For the generic models, we have experimented with two ways of community placement: in a tiered fashion (as shown in TP2 in Fig. 2), or in a random fashion. Our discrete-time simulator is written in C++. More details about the simulator, as well as the source code, can be found at [30].

#### A. The Nodal Spatial Distribution

To observe the nodal spatial distribution, we divide the simulation area into a 20-by-20 grid and count the average number of nodes in each grid block during the simulation. The results presented in this subsection is the average of 5000 runs of independent simulations.

If the communities are randomly chosen, the node should appear at each of the 400 evenly divided grid equal likely, with probability 1/400. We observe that the spatial distribution of node varies a bit about this value in the simulation, as shown in Fig. 7 (a). The minor discrepancy is due to the finite number of samples. To make the scenario more interesting, we also generate the spatial distribution for nodes when the communities are fixed. We use the parameter sets of Model 1 (one community in each time period) and Model-5 (two-tier community in each time period), and assign the center of the community at either (300,300) or (700,700) with one half probability. The resulting nodal spatial distributions are shown in Fig. 7 (b) and (c), respectively. The node appears with higher probability where the communities are assigned. From Eq. (3), we derive the theoretical values for the spatial distributions. In both cases the simulation results follow the theoretical results reasonably well, within about 10% error.

#### B. The Average Node Degree

For the average node degree, we create simulation scenarios with 50 nodes in the simulation area, and calculate the average node degree of each node by taking the time average across snapshots taken every second during the simulation, and then average across all nodes. All the runs last for 60000 seconds in this subsection.

As we show in Corollary 5.5, when the communities are randomly chosen, the average node degree turns out to be the average number of nodes falling in the communication range of a given node, as if all nodes are uniformly distributed. Hence the average node degree does not depend on the exact choices of community setup (i.e. single, multiple, or multi-tier communities) or other mobility parameters. In Fig. 8 (a), we see the simulation curves follow the prediction of the theory well.

Again, to make the scenario a bit more realistic, we simulate some more scenarios when the communities are fixed. Among the 50 nodes, we make 25 of them pick the community centered at (300,300) and the other 25 pick the community centered at (700,700). We simulate scenarios for all seven sets of parameters, and show some example results in Fig. 8 (b). In the simulations, when the communication ranges are small as compared to the edge of the communities, the relative errors are low, indicating a good match between the theory and the simulation. However, as the communication range increases, the area covered by the communication disk becomes comparable to the size of the community and Eq. (5) is no longer accurate since the communication disk extends out of the overlapped area in most cases. That is the reason for the discrepancies between the theory and simulation. Besides Model-3, we observe at most 20% of error when the communication disk is less than 20% the size of the innermost community, indicating that our theory is valid when the communication range is relatively small.

#### C. The Hitting Time and the Meeting Time

We perform simulations for the hitting and the meeting times for 50,000 independent iterations for each scenario, and compare the average results with the theoretical values derived from the corresponding equations (i.e. (7) and (16)). To find out the hitting or the meeting time, we move the nodes in the simulator indefinitely until they hit the target or meet with each other, respectively.

Again we show some example results in Fig. 9. For all the scenarios (including the ones not listed here), the relative
errors are within acceptable range. The absolute values for the error are within 16% for the hitting time and within 20% for the meeting time. For more than 70% of the tested scenarios, the error is below 10% (refer to [30] for other figures). These results display the accuracy of our theory under a wide range of parameter settings. The errors between the theoretical and simulation results are mainly due to some of the approximations we made in the various derivations. For example, there exist some border effects with respect to the hitting and meeting probabilities within a community. When a node is close to the border of a community, it could also “see” some other nodes outside of the community if its transmission range is large enough. However, we have chosen to ignore such occurrences to keep our analysis simpler. Furthermore, the approximation of the hitting and meeting processes with discrete Bernoulli trials is valid only for the epochs that are large enough (in the order of community size). Nevertheless, as shown in the figures, the errors are always within acceptable ranges, justifying our simplifying assumptions.

VII. USING THEORY FOR PERFORMANCE PREDICTION

Although the various theoretical quantities derived for the TVC model in Section V are interesting in their own merit, they are particularly useful in predicting protocol performance, which in turn can guide the decisions of system operation. We illustrate this point with two examples in this section.

A. Estimation of the Number of Nodes Needed for Geographic Routing

It has been shown in geographic routing that the average node degree determines the success rate of messages delivered [34]. Thus, using the results of Section V-B we can estimate the number of nodes (as a function of the average node degree) needed to achieve a target performance for geographic routing, for a given scenario.

We consider the same setup as in Section VI-B, where half of the nodes are assigned to a community centered at (300, 300) and the other half are assigned to another community centered at (700, 700). We are interested in routing messages across one of the communities, from coordinate (250, 250) to coordinate (350, 350) with simple geographic routing (i.e., greedy forwarding only, without face routing [35]). Using simulations we obtain the success rate of geographic routing under various communication ranges when 200 nodes move according to the mobility parameters of Model-I (Table II). Results are shown in Fig. 10 (each point is the percentage of success out of 2000 trials). If we assume the mobility model is different, say Model-3, we would like to know how many nodes we need to achieve similar performance. Using Eq. (6) we find that 760 nodes are needed to create a similar average node degree for Model-3. To validate this, we also simulate geographic routing for a scenario where 760 nodes follow Model-3. Comparing the resulting message delivery ratio for this scenario to the original scenario (200 nodes with Model-I) in Fig. 10, we see that similar success rates are achieved under the same transmission range, which confirms the accuracy of our analysis.

B. Predicting Message Delivery Delay with Epidemic Routing

Epidemic routing is a simple and popular protocol that has been proposed for networks where nodal connectivity is intermittent (i.e., in Delay Tolerant Networks) [32]. It has been shown that message propagation under epidemic routing can be modeled with sufficient accuracy using a simple fluid-based model [33]. (Note that its performance has also been analyzed using Markov Chain [19] and Random Walk [4] models.) This fluid model has been borrowed from the Mathematical Biology community, and is usually referred to as the SI (Susceptible-Infected) epidemic model. The gist of the SI model is that the rate by which the number of “infected” nodes increases (“infected” nodes here are nodes who have received a copy of the message) can be approximated by the product of three quantities: the number of already infected nodes, the number...
of susceptible (not yet infected) nodes, and the pair-wise contact rate, $\beta$ (assuming nodes meet independently – this contact rate is equivalent to the unit-step meeting probabilities calculated in (14)). Thus, one could plug-in these meeting probabilities into the SI model equations and calculate the delay for epidemic routing. Yet, in the TVC model (and often in real life) there are multiple groups of nodes with different communities, and thus different pair-wise contact rates that depend on the community setup. For example, nodes with the same or overlapping communities tend to meet much more often than nodes in far away communities. For this reason, we extend the basic SI model to a more general scenario that is applicable to the TVC model.

We consider the following setup in the case study: We use Model-3 (Table II) for the mobility parameters. A total of $M = 50$ nodes are divided into two groups of 25 nodes each. One group has its community centered at (300, 300) and the other at (700, 700). One packet starts from a randomly picked source node and the time needed until it reaches all other nodes in the network using epidemic routing is calculated. The propagation of the message can be described by the following equations:

\[
\begin{align*}
\frac{dI_1(t)}{dt} & = \beta_{ov}I_1(t)S_1(t) + \beta_{no-ov}I_2(t)S_1(t) \\
\frac{dI_2(t)}{dt} & = \beta_{ov}I_2(t)S_2(t) + \beta_{no-ov}I_1(t)S_2(t) \\
S_1(t) + I_1(t) & = M/2 \\
S_2(t) + I_2(t) & = M/2.
\end{align*}
\] (19)

where $S_x(t)$ and $I_x(t)$ denote the number of susceptible and infected nodes at time $t$ in group $x$, respectively. Parameters $\beta_{ov}$ and $\beta_{no-ov}$ represent the pair-wise unit-time meeting probability when the communities are overlapped (i.e., for nodes in the same group) and not overlapped (i.e., nodes in different groups), respectively. We use Eq. (14) to obtain these quantities. This model is an extension from the standard SI model [33] and similar extensions can be made for more than two groups [41]. The first equation governs the change of infected nodes in the first group. Notice that the infection to susceptible nodes in the group ($S_1(t)$) can come from the infected nodes in the same group ($I_1(t)$) or the other group ($I_2(t)$). We can solve the system of equations in (19) to get the evolution of the total infected nodes in the network. As can be seen in Fig. 11, the theory curve closely follows the trend in the simulation curve (the non-perfect matching between the two curves, is due to the fact that fluid models become more accurate approximations of the actual stochastic spreading for large numbers of nodes). This indicates first that scenarios generated by our mobility model are still amenable to fluid model based mathematical analysis (SI), despite the increased complexity introduced by the concept of communities. It also shows that results produced thus can be used by a system designer to predict how fast messages propagate in a given network environment. This might, for example, determine if extra nodes are needed in a wireless content distribution network to speed up message dissemination.

As a final note, in addition to epidemic routing, the theoretical results for the hitting and meeting times could be applied to predict the delay of various other DTN routing protocols (see e.g. [18], [4], [33]), for a large range of mobility scenarios that can be captured by the TVC model.

VIII. CONCLUSION AND FUTURE WORK

We have proposed a time-variant community mobility model for wireless mobile networks. Our model preserves common mobility characteristics, namely skewed location visiting preferences and periodical re-appearance at the same location. We have tuned the TVC model to match with the mobility characteristics of various traces (WLAN traces, a vehicle mobility trace, and an encounter trace of moving human beings), displaying its flexibility and generality. A mobility trace generator of our model is available at [30]. In addition to providing realistic mobility patterns, the TVC model can be mathematically analyzed to derive several quantities of interest: the nodal spatial distribution, the average node degree, the hitting time and the meeting time. Through extensive simulation studies, we have verified the accuracy of our theory.

The TVC model can be easily generalized to provide scenarios in which nodes display more heterogeneous behavior. Nodes may have different set of parameters and even the time period structure can be different for different nodes. With these extensions, we have a mobility model to describe an environment including users with diverse mobility characteristics. We believe such a model is a very important building block for understanding protocol performances in real-life settings. To demonstrate this last point, we also provide some examples of how our theory can be used in practice to predict protocol performance and guide design decisions.

In the future we would like to further analyze the performance of various routing protocols (e.g., [4], [5]) under the time-variant community mobility model. We also would like to construct a systematic way to automatically generate the configuration files, such that the communities and time periods of nodes are set to capture the inter-node encounter properties we observe in various traces (for example, the Small World encounter patterns observed in WLAN traces [38]).

REFERENCES


[27] Simulation codes used in this work and its detailed description are available at http://nile.cise.uff.br/weijsenbs/TVC_model.


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