

MATH 445 ASSIGNMENT 3
Fall 2009
Prof. Alexander

Due Friday September 18.

Kreyszig:

11.1 p. 483 #2, 7, 9, 12, 13, 17

11.2 p. 490 #2, 3, 5

11.3 p. 496 #1, 4, 12, 16, 18, 25

Some even-numbered solutions:

$$\mathbf{11.2} \quad (2) \quad 2 + \frac{8}{\pi} \left(\sin \frac{\pi x}{2} + \frac{1}{3} \sin \frac{3\pi x}{2} + \frac{1}{5} \sin \frac{5\pi x}{2} + \dots \right)$$

$$\mathbf{11.3} \quad (12) \quad \frac{4}{\pi^3} \left((\pi^2 - 4) \sin \pi x + \frac{1}{27} (9\pi^2 - 4) \sin 3\pi x + \frac{1}{125} (25\pi^2 - 4) \sin 5\pi x + \dots \right) \\ - \frac{2}{\pi} \left(\sin 2\pi x + \frac{1}{2} \sin 4\pi x + \frac{1}{3} \sin 6\pi x + \dots \right)$$

$$(16) \quad \frac{1}{4} + \frac{4}{\pi^2} \left(\cos \frac{\pi x}{4} + \frac{1}{2} \cos \frac{2\pi x}{4} + \frac{1}{9} \cos \frac{3\pi x}{4} + \frac{1}{25} \cos \frac{\pi x}{4} + \frac{1}{18} \cos \frac{6\pi x}{4} + \frac{1}{49} \cos \frac{7\pi x}{4} + \dots \right)$$

$$(18)(a) \quad \frac{1}{4} - \frac{2}{\pi^2} \left(\cos 2\pi x + \frac{1}{9} \cos 6\pi x + \frac{1}{25} \cos 10\pi x + \frac{1}{49} \cos 14\pi x + \dots \right)$$

$$(b) \quad \frac{1}{\pi} \left(\sin 2\pi x - \frac{1}{2} \sin 4\pi x + \frac{1}{3} \sin 6\pi x - \frac{1}{4} \sin 8\pi x + \dots \right)$$

When you can do so readily, you should express answers in series notation, for example,

$$3 + \sum_{n=1}^{\infty} \left(\frac{(-1)^n}{n^2} - 2 \right) \cos nx + \sum_{n \text{ even}} \frac{1}{2n} \sin nx.$$

If this cannot be readily done, then you can express your answer as in the solutions above, calculating enough terms to make the pattern clear.